Year 6

# Calculation policy

Updated September 2024



#### **Guidance for teachers**

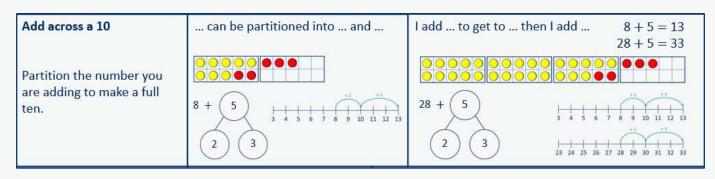


The calculation policy is divided into four sections: addition, subtraction, multiplication and division. At the start of each section, you will find an overview of the progression of skills. Calculations involving decimal numbers and fractions are included.

The calculation policy follows the same concrete, pictorial, abstract approach as our main schemes of learning. Where appropriate, sentence stems and key questions are included alongside the key representations.

Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.



# Progression of skills – Addition



Year 5	Year 6
Add using mental strategies	Add integers up to 10 million
Add whole numbers with more than 4 digits	Add decimals with up to 3 decimal places
Add decimals with up to 2 decimal places	Order of operations
Complements to 1	Negative numbers
Add fractions with denominators that are a multiple of one another	Add fractions



Year 6	• (	Add Use 4 op Calc Add equi	the eratulat	ir k tio te i ctio	novns. ntei	wled rval: with	dge s ac	of t	he s ze	ordo ro.	er (	of o <sub>l</sub>	per	ati	ons	to	ca	arr	y c	out	cald	cula	itio	ns	inv	olv/		the t of
Progression of skills	Key	repr	ese	enta	atio	ns																						
Add integers up to 10																												
million			2	1	6	2	2	1												Г		T		T				
Encourage children to		-	-	4	6	2	2	1														8	1	T		8	5	
estimate and use inverse				8	4	3	2	1													+				0	6		
operations to check answers				3	0	5	4	2						?								ç	9	)	5		8	
to calculations.		14 25	1	1								2,354	4	7	750	1	.,50	00					L					
Add decimals with up to 3 decimal places	I do/	1	not Tth	ï	ed t	O M		e an	exc	har	nge	e bed	cau	ise														
Progress to numbers with digits in different place value columns.	00					2001 (2001 2001) (2001 2001) (2001	0001												_									
Encourage children to check that they have lined up the columns correctly.	5		2		<u></u>	2	0.001		+	3 · 1 2 · 1 5 · 2	5	4					+	2	9	. 5	2 7 8 0 7							



Progression of skills	Key representations										
Order of operations	has greater priority than, so the first part of the calculation I need to do is										
Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets are shown and the operations have the same priority, work left to right.	powers $(3 + 4) \times 2$ $\times \text{ and } \div$ $+ \text{ and } -$	$2 = 14$ $3 + 4 \times 2 = 11$ $3 \times 4 + 2 = 14$									
Negative numbers  Children add to negative numbers and carry out calculations which cross 0	plus is equal to $-3 + 5 = 2$ $-5 -4 -3 -2 -1 0 1 2 3 4 5$	-5 $-4$ $-3$ $-2$ $-1$ 0 1 2 3 4 5  The difference between $-5$ and $-1$ is 4									
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	+5 $+5$ $-5$ $0$ $5$ The difference between $-5$ and $5$ is $10$									



Progression of skills	Key representations		
Add fractions	The denominator has been multiplied by, so the	The lowest common multiple of and is	is made up of wholes and
Convert fractions to the	numerator needs to be		
same denominator before	multiplied by		
adding. Progress from fractions where one			
denominator is a multiple of		$\left(\frac{1}{3}\right)\left(\frac{1}{4}\right)$	$\left(2\frac{2}{3}\right)\left(1\frac{1}{6}\right)$
the other, to any fractions and then to mixed numbers.	$\left(\frac{1}{3}\right)\left(\frac{5}{12}\right)$		
and then to mixed numbers.			
		$\frac{1}{3} + \frac{1}{4} = \frac{4}{13} + \frac{3}{13} = \frac{7}{13}$	

# **Progression of skills - Subtraction**



Year 5	Year 6
Subtract whole numbers with more than 4 digits	Subtract integers up to 10 million
Subtract using mental strategies	Subtract decimals with up to 3 decimal places
Subtract decimals with up to 2 decimal places	Order of operations
Complements to 1	Negative numbers
Subtract fractions with denominators that are a multiple of one another	Subtract fractions



Year 6	• L	<ul> <li>Use their knowledge of the order of operations to carry out calculations involving the 4 operations.</li> <li>Calculate intervals across zero.</li> </ul>																						
Progression of skills	Кеу і	repres	sent	atio	ns																			
Subtract integers up to 10 million																								
- 191		<sup>2</sup> ,3′	<sup>1</sup> 4	<sup>5</sup> 8	<sup>1</sup> 2	2	1																	
Encourage children to estimate and use inverse		- 1	8	4	3	2	1											8		4	8	5		
operations to check answers		1	6	1	9	0	0					4,60	)4			1	-	3	5	5	5	5	5	
to calculations.										2,35	64	75		?					J		J	J	J	
Subtract decimals with up to 3 decimal places  Progress from the same number of decimal and whole number places to a different number of decimal and whole number places.	I do/	6 <sup>6</sup> 7 1 · 3 5 · 3	<sup>1</sup> 3 4	ed t	o m	nake	e an		har Tth		h	Thth			0 x 1.5 0 ·									



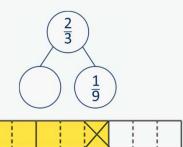
Progression of skills	Key representations										
Order of operations	has greater priority than, so the first part of the calculation I need to do is										
Children learn the order of priority for operations in a calculation. Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.	powers $\begin{array}{c} \times \text{ and } + \\ + \text{ and } - \\ \end{array}$ $(8-2) \times 3 = 18$										
Negative numbers  Children subtract from positive and negative numbers and calculate	minus is equal to $-1-4=-5$ $-5-4-3-2-1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5$ The difference between $-5$ and $-1$ is $4$										
intervals across 0	1 - 4 = -3 $-5$ $-5$ $-5$ $-5$ $-5$ $-5$ $-5$ $-5$										



# Progression of skills Key representations Subtract fractions The denominator has

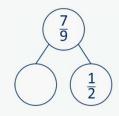
Convert fractions to the same denominator before subtracting. Progress from fractions where one denominator is a multiple of the other, to any fractions and then subtracting from a mixed number.

The denominator has been multiplied by ..., so the numerator needs to be multiplied by...



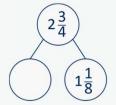
$$\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$$

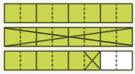
The lowest common multiple of ... and ... is ...



$$\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$$

... is made up of ... wholes and ...





$$2\frac{3}{4} - 1\frac{1}{8} = 1\frac{5}{8}$$

# Progression of skills – Multiplication



Year 5	Year 6
Multiples and factors	Multiply numbers up to 4 digits by a 2-digit
Square and cube numbers	number
Multiply numbers up to 4 digits by a 1-digit	Multiply by 10, 100 and 1,000
number	Order of operations
<ul> <li>Multiply numbers up to 4 digits by a 2-digit number</li> </ul>	Multiply decimals by integers
	Multiply fractions by fractions
• Multiply by 10, 100 and 1,000	Find the whole
Mental strategies	Calculations involving ratio
Multiply fractions by a whole number	
Multiply mixed numbers by a whole number	
Find the whole	



Year 6	<ul> <li>Identify common factors and common multiples.</li> <li>Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication.</li> <li>Multiply numbers by 10, 100 and 1,000</li> <li>Multiply one-digit numbers with up to two decimal places by whole numbers.</li> <li>Use their knowledge of the order of operations to carry out calculations involving the 4 operations.</li> <li>Multiply simple pairs of proper fractions, writing the answer in its simplest form.</li> <li>Solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts.</li> <li>Solve problems involving the calculation of percentages.</li> </ul>								
Progression of skills	Key representations								
Multiply numbers up to 4 digits by a 2-digit number	To multiply by a 2-digit number, first multiply by the ones, then multiply by the tens and then find the total. $\begin{array}{c ccccccccccccccccccccccccccccccccccc$								
Multiply by 10, 100 and 1,000 Some children may overgeneralise that multiplying by a power of 10 always results in adding zeros.	To multiply by $10/100/1,000$ , I move all the digits places to the left is $10/100/1,000$ times the size of  M HTh TTh Th H T O Tth Hth Thth  234 × 10 = 2,340  234 × 100 = 23,400  0.234 × 100 = 23.4  234 × 1,000 = 234,000  0.234 × 1,000 = 234								



Progression of skills	Key representations
Order of operations  Calculations in brackets should be done first.  Multiplication and division should be performed before addition and subtraction.	has greater priority than, so the first part of the calculation I need to do is $(3+4)\times 2=14$ $3+4\times 2=11$
Multiply decimals by integers  This is the first time children multiply decimals by numbers other than 10, 100 or 1,000 Encourage them to make links with known facts and whole number multiplication.	I know that $\times$ $=$ , so I also know that $\times$ $=$ I need to exchange 10 for 1  I need to exchange 10 for 1 $6 \times 2 = 12$ $6 \times 0.2 = 1.2$ I need to exchange 10 for 1 $6 \times 2 = 12$ $6 \times 0.2 = 1.2$



Progression of skills	Key representations	
Multiply fractions by fractions	When multiplying a pair of fractions, I ne denominator.	ed to multiply the numerator and multiply the
Encourage children to give answers in their simplest form.		
	$\frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$ $\frac{2}{3} \times \frac{4}{5} = \frac{8}{15}$	$\frac{2}{3} \times \frac{3}{5} = \frac{6}{15} = \frac{2}{5}$
Find the whole	If $\frac{1}{\Box}$ is, then the whole is $\times$	If $\Box$ is, then $\frac{1}{\Box}$ is and the whole is $\times$
Children multiply to find the whole from a given part.	$\frac{1}{3}$ of = 18  ? $18 \times 3 = 54$ $\frac{1}{3}$ of <b>54</b> = 18	$\frac{4}{9} \text{ of } \underline{\hspace{0.5cm}} = 48$ $\frac{1}{9} = 48 \div 4 = 12$ $9 \times 12 = 108$ $\frac{4}{9} \text{ of } 108 = 48$



Progression of skills	Key representations	
Calculate percentages	There are lots of % in 100% To find %, I need to divide by	% is made up of %, and %
Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.	100% 50% 50% 25% 25% 25% 25% 25% 50% of = ÷ 2	100% 10% 10% 10% 10% 10% 10% 10% 10% 10% 10%  To find 30%, I can find 10% and then multiply it by 3 To find 23%, I can use 10% × 2 and 1% × 3  To find 00% I can find 1% then subtract from 100%
Calculations involving ratio	25% of = $\div$ 4 For every , there are	To find 99%, I can find 1%, then subtract from 100%
Encourage children to see the multiplicative	For every 1 adult on a school trip, th	ere are 6 children.  Adults Children
relationship between ratios. They will need to multiply or divide each value by the	adults	1 6 2 12 × 3 3 18
same number to keep the ratio equivalent.  Double number lines and	children	×6
ratio tables help children to see both horizontal and vertical multiplicative relationships.	The ratio of adults to children is 1 :	0 1 2 3 4 5 6 Adults

# Progression of skills – Division



Year 5	Year 6
Mental strategies	Short division
Divide numbers up to 4 digits by a 1-digit	Mental strategies
number	Long division
• Divide by 10, 100 and 1,000	Order of operations
Fraction of an amount	• Divide by 10, 100 and 1,000
	Divide decimals by integers
	Decimal and fraction equivalents
	Divide a fraction by an integer
	Fraction of an amount
	Calculate percentages
	Calculations involving ratio



Year 6	<ul> <li>Perform mental calculations, including with mixed operations and large numbers.</li> <li>Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.</li> <li>Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.</li> <li>Divide numbers by 10, 100 and 1,000 giving answers up to three decimal places.</li> <li>Use written division methods in cases where the answer has up to two decimal places.</li> <li>Associate a fraction with division and calculate decimal fraction equivalents.</li> <li>Divide proper fractions by whole numbers [for example, 1/3 ÷ 2 = 1/6]</li> <li>Solve problems involving the calculation of percentages.</li> </ul>
Progression of skills	Key representations
Short division  Encourage children to interpret remainders in context, for example knowing that "4 remainder 1" could mean 4 complete boxes with 1 left over so 5 boxes will be needed.	There are groups of hundreds/tens/ones/ in I can exchange 1 for 10  There are groups of hundreds/tens/ones/ in  The exchange 1 for 10  The excha



Progression of skills	Key representations				
Mental strategies	To divide by, I can first divide by and then divide the answer by				
Include partitioning and number line strategies outlined in Y5 as well as division using factors.	$240 \div 60 = 240 \div 10 \div 6$ $240 \rightarrow \begin{array}{c} \div 10 \\ \hline \end{array} $ $480 \div 24 = 480 \div 4 \div 6$ $480 \rightarrow \begin{array}{c} \div 4 \\ \hline \end{array} $ $9,120 \div 15 = 9,120 \div 5 \div 3$ $9,120 \\ \hline \end{array} $ $15 = 9,120 \div 5 \div 3$ $17 = 9,120$ $17 = 9,$				
Long division  The long division method is introduced for the first time. Two alternative methods are shown.	Method 1    0   3   6     0   2   4   r   12     15   3   7   2	Method 2    0   3   6     0   1   0   9   r   9     13   1   4   2   6			
Order of operations Calculations in brackets should be done first, then powers. Multiplication and division should be performed before addition and subtraction.	has greater priority than, so the first part of powers $\times$ and $\div$ $+$ and $ (6+4) \div 2 =$				

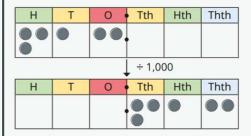


#### **Progression of skills Key representations**

#### Divide by 10, 100 and 1,000

Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.

To divide by ..., I move the digits ... places to the right.



$$312 \div 10 = 31.2$$
  
 $312 \div 100 = 3.12$   
 $312 \div 1,000 = 0.312$ 

$$906 \div 10 = 90.6$$
  
 $906 \div 100 = 9.06$   
 $906 \div 1,000 = 0.906$ 

#### **Divide decimals by integers**

This is the first time children divide decimals by numbers other than 10, 100 or 1,000

I know that  $... \div ... = ...$ so I also know that  $\dots \div \dots = \dots$ 

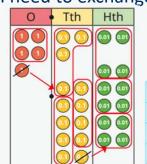


 $39 \div 3 = 13$ 

$$3.9 \div 3 = 1.3$$

$$0.39 \div 3 = 0.13$$

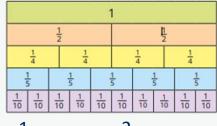
#### I need to exchange 1 ... for 10 ...



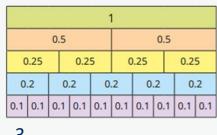


#### **Decimal and fraction** equivalents

The fraction ... is equivalent to the decimal ...

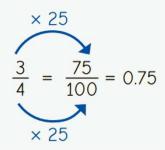


$$\frac{1}{5} = 0.2$$
  $\frac{2}{5} = 0.4$ 



$$\frac{3}{5} = 0.6$$







Progression of skills	Key representations			
Divide a fraction by an integer	ones divided by 2 is ones so sevenths divided by 2 is sevenths.	I am dividing by, so I can split each part into equal parts.	is equivalent to so $\div$ $=$ $\div$	
This is the first time children divide fractions by an integer.	$\frac{4}{7} \div 4 = \frac{1}{7}$ $\frac{4}{7} \div 2 = \frac{2}{7}$	$\frac{1}{3} \div 2 = \frac{1}{6}$	$\frac{2}{3} = \frac{4}{6}$ so $\frac{2}{3} \div 4 = \frac{4}{6} \div 4 = \frac{1}{6}$	
Fraction of an amount  Children divide and multiply	To find $\frac{1}{\Box}$ I divide by	If $\frac{1}{\Box}$ is equal to, then $\frac{\Box}{\Box}$ are equal to	If is equal to, then the whole is equal to	
to find fractions of an amount. Bar models can still be used to support understanding where needed.	$\frac{1}{2} \text{ of } 36 = 36 \div 2$ $\frac{1}{12} \text{ of } 36 = 36 \div 12$	$\frac{2,700 \text{ m}}{7}$ $\frac{7}{9} \text{ of } 2,700 = \frac{1}{9} \text{ of } 2,700 \times 7$	$\frac{4}{9} \text{ of } \underline{\qquad} = 48$	



Progression of skills	Key representations				
Calculate percentages  Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.	There are lots of % in 100% To find %, I need to divide by $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	% is made up of %, and %  100% 10% 10% 10% 10% 10% 10% 10% 10% 10% 10%			
Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent.  Double number lines and	For every , there are  For every 6 children on a school tri adults  children	p, there is 1 adult.  Adults Children $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			
ratio tables help children to see both horizontal and vertical multiplicative relationships.	The ratio of children to adults is 6 :	0 1 2 3 4 5 6 Adults Children 0 6 12 18			

Year 5

# Calculation policy

Updated September 2024



#### **Guidance for teachers**

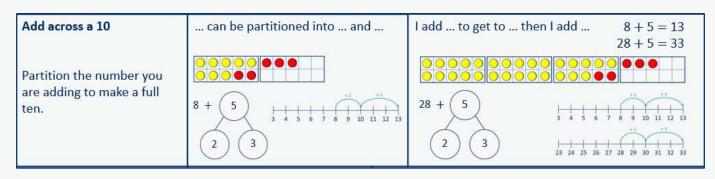


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The calculation policy follows the same concrete, pictorial, abstract approach as our main schemes of learning. Where appropriate, sentence stems and key questions are included alongside the key representations.

Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.



# Progression of skills – Addition



Year 4	Year 5	Year 6
<ul> <li>Add 1s, 10s and 100s to a 4-digit number</li> <li>Add up to two 4-digit numbers</li> <li>Add decimal numbers in the context of money</li> <li>Add fractions and mixed numbers with the same denominator beyond 1 whole</li> </ul>	<ul> <li>Add using mental strategies</li> <li>Add whole numbers with more than 4 digits</li> <li>Add decimals with up to 2 decimal places</li> <li>Complements to 1</li> <li>Add fractions with denominators that are a multiple of one another</li> </ul>	<ul> <li>Add integers up to 10 million</li> <li>Add decimals with up to 3 decimal places</li> <li>Order of operations</li> <li>Negative numbers</li> <li>Add fractions</li> </ul>



Year 5	<ul> <li>Add whole numbers with more than 4 digits, including using formal written methods.</li> <li>Add numbers mentally with increasingly large numbers.</li> <li>Add decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1</li> <li>Add fractions with the same denominator, and denominators that are multiples of the same number.</li> </ul>
Progression of skills	Key representations
Add using mental strategies  Add 1s, 10s, 100s, etc. to any number.  Use number bonds and related facts.	TTh Th H T O
Add whole numbers with more than 4 digits  Encourage children to estimate and use inverse operations to check answers to calculations.	I can exchange 10 for 1  The property of the property



#### **Progression of skills Key representations** Add decimals with up to 2 I do/do not need to make an exchange because ... decimal places I can exchange 10 ... for 1 ... Thth Tth Hth 1 . 2 8 1 001 001 000 Progress from the same + 2 - 5 4 **600 600** number of decimal places to 0.01 Tenths Hundredths Ones a different number of **600** 4 • 4 5 0.01 0.01 decimal places, and from no 0.01 0.01 3 • 2 1 10 000 001 exchange to exchange. 000 0.01 **600 Complements to 1** 0.3 +0.35 +Pairs of numbers with up to 3 decimal places which total 1 1 0.44 0.444 0.4 Encourage children to make links with bonds to 10 and 0.4 + 0.6 = 14 + 6 = 10complements to 100 and 71 0.71 44 + 56 = 1000.44 + 0.56 = 11,000 100 444 + 556 = 1,0000.444 + 0.556 = 1



Progression of skills	Key representations		
Add fractions with denominators that are a multiple of one another	The denominator has been multiplied by, so the for the fractions to be equivalent.	enominator has been multiplied by, so the numerator needs to be multiplied by e fractions to be equivalent.	
Encourage children to convert fractions to the same denominator before adding.	$\frac{1}{2} + \frac{1}{8} = \frac{4}{8} + \frac{1}{8} = \frac{5}{8}$		
Progress from adding fractions within 1 whole to adding fractions beyond 1 whole.	$\frac{1}{4} + \frac{3}{8} = \frac{2}{8} + \frac{3}{8} = \frac{5}{8}$	$\frac{3}{4} + \frac{5}{8} = \frac{6}{8} + \frac{5}{8} = \frac{11}{8} = 1\frac{3}{8}$	

# **Progression of skills - Subtraction**



Year 4	Year 5	Year 6
<ul> <li>Subtract 1s, 10s, 100s and 1,000s from a 4-digit number</li> </ul>	<ul> <li>Subtract whole numbers with more than 4 digits</li> </ul>	Subtract integers up to 10 million
<ul> <li>Subtract up to two 4-digit numbers</li> </ul>	<ul> <li>Subtract using mental strategies</li> </ul>	Subtract decimals with up to 3 decimal places
<ul> <li>Subtract decimal numbers in the context of money</li> <li>Subtract fractions and mixed numbers with the same denominator</li> </ul>	<ul> <li>Subtract decimals with up to 2 decimal places</li> <li>Complements to 1</li> <li>Subtract fractions with denominators that are a multiple of one another</li> </ul>	<ul> <li>Order of operations</li> <li>Negative numbers</li> <li>Subtract fractions</li> </ul>



Year 5	<ul> <li>Subtract whole numbers with more than 4 digits.</li> <li>Subtract numbers mentally with increasingly large numbers.</li> <li>Subtract decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1</li> <li>Subtract fractions with the same denominator, and denominators that are multiples of the same number.</li> </ul>
Progression of skills	Key representations
Subtract whole numbers with more than 4 digits  Encourage children to estimate and use inverse operations to check answers to calculations.	I can exchange 1 for 10  TTh Th H T 0  2 3 11 5 13 4  - 3 2 7 4  - 1 2 2 0 8 5 8  2 8 2 6 0
Subtract using mental strategies  Subtract 1s, 10s, 100s etc from any number. Use number bonds and related facts.	TTh Th H T O Subtract, I can subtract then add  48,650 - 300 = 48,650 - 30,000 = 48,650 - 30 = 6,458 6,459  6,458 6,459  6,558



#### **Progression of skills**

#### Subtract decimals with up to 2 decimal places

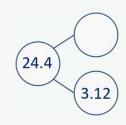
Progress from the same number of decimal places to a different number of decimal places and from no exchange to exchange.

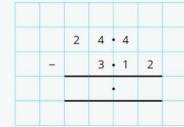
#### **Key representations**



0.35 +

	24.4
3.12	?



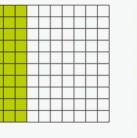


0.444

#### **Complements to 1**

Encourage children to make links with bonds to 10 and complements to 100 and 1,000 when finding a missing part or subtracting from 1



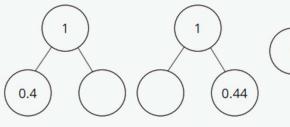


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= 1

	10		100	
3	?	35	?	
	1		1	
0.3	?	0.35	?	







$$10 - 4 = 6$$
  $1 - 0.4 = 0.6$ 

$$100 - 44 = 56$$

$$100 - 44 = 56$$
  $1 - 0.44 = 0.56$ 

$$1,000 - 444 = 556$$
  $1 - 0.444 = 0.556$ 

$$1 - 0.444 = 0.556$$



#### Progression of skills Key representations

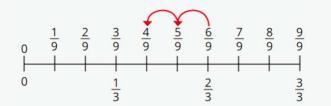
Subtract fractions with denominators that are a multiple of one another

Convert fractions to the same denominator before subtracting. Progress from subtracting fractions within 1 whole to subtracting from a mixed number.

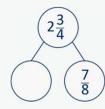
The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.



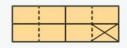
$$\frac{1}{3} - \frac{1}{15} = \frac{5}{15} - \frac{1}{15} = \frac{4}{15}$$



$$\frac{2}{3} - \frac{2}{9} = \frac{6}{9} - \frac{2}{9} = \frac{4}{9}$$









# Progression of skills – Multiplication



Year 4	Year 5	Year 6
• Times-table facts to $12 \times 12$	Multiples and factors	Multiply numbers up to 4     digits by a 2-digit number
<ul><li>Multiply by 1 and 0</li><li>Multiply 3 numbers</li></ul>	<ul><li>Square and cube numbers</li><li>Multiply numbers up to 4</li></ul>	<ul> <li>Multiply by 10, 100 and 1,000</li> </ul>
• Factor pairs	digits by a 1-digit number	Order of operations
Multiply by 10 and 100	<ul> <li>Multiply numbers up to 4 digits by a 2-digit number</li> </ul>	<ul><li>Multiply decimals by integers</li><li>Multiply fractions by fractions</li></ul>
Related facts	• Multiply by 10, 100 and 1,000	Find the whole
<ul> <li>Mental strategies</li> <li>Multiply a 2 or 3-digit number</li> </ul>	<ul> <li>Mental strategies</li> </ul>	Calculations involving ratio
<ul> <li>Multiply a 2 or 3-digit number</li> <li>by a 1-digit number</li> </ul>	<ul> <li>Multiply fractions by a whole number</li> </ul>	
Scaling	<ul> <li>Multiply mixed numbers by a whole number</li> </ul>	
Correspondence problems	<ul> <li>Find the whole</li> </ul>	



Year 5	<ul> <li>Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers</li> <li>Recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³)</li> <li>Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers.</li> <li>Multiply numbers mentally drawing upon known facts.</li> <li>Multiply whole numbers and those involving decimals by 10, 100 and 1000</li> <li>Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.</li> </ul>		
Progression of skills	Key representations		
Multiples and factors  Encourage children to notice patterns and make links with known facts.	is a multiple of because × =  1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	is a factor of because × =  1 × 8  2 × 4  1, 2, 4 and 8 are factors of 8	The common factors of and are  Factors of 20 Factors of 12  5 1 2 3 6 12
Square and cube numbers	squared means $\times$ 1 × 1 2 × 2 3 × 3  1 <sup>2</sup> = 1 2 <sup>2</sup> = 4 3 <sup>2</sup> = 9		$\times \times$ $2 \times 2$ $3 \times 3 \times 3$ $= 8$ $3^3 = 27$



Progression of skills	Key representations	
Multiply numbers up to 4 digits by a 1-digit number  This builds on the short multiplication method introduced in Y4	To multiply a 4-digit number by , I mul by and the thousands by	tiply the ones by , the tens by , the hundreds  Th H T O 1 1 1 5 2
Multiply numbers up to 4 digits by a 2-digit number  Numbers are first partitioned using an area model then long multiplication is introduced for the first time.	I can partition into and $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	First, I multiply by the Then I multiply by the    X   10   3     3   2     3   2



Progression of skills	Key representations	
Multiply by 10, 100 and 1,000	To multiply by 10/100/1,000, I move all the digits places to the left is 10/100/1,000 times the size of	
Some children may over- generalise that multiplying by a power of 10 always results in adding zeros. This will cause issues later when multiplying decimals.	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Mental strategies  Children continue to use efficient mental strategies such as partitioning and knowledge of factor pairs and related facts to multiply.	The most efficient strategy to calculate $\times$ is To calculate $\times$ 12, I can do $\times$ $\times$ For example: $121 \times 12$ I could calculate $100 \times 12$ plus $20 \times 12$ plus $1 \times 12$ I could calculate $121 \times 10$ plus $121 \times 2$ I could calculate $121 \times 6 \times 2$ I could calculate $121 \times 4 \times 3$	



Progression of skills	Key representations	
Multiply fractions by a whole number	To multiply a fraction by an integer, I multiply the numerator by the integer and the denominator remains the same.	
Make links with repeated addition. E.g. $\frac{1}{5} \times 4 = \frac{1}{5} + \frac{1}{5} + \frac{1}{5} + \frac{1}{5}$	$\frac{1}{7} \frac{1}{7} \frac{1}{7} \frac{1}{7} \frac{1}{7} \frac{1}{7}$ $\frac{1}{7} \times 5 = \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} = \frac{5}{7}$ $\frac{2}{7} \times 3 = \frac{2}{7} + \frac{2}{7} + \frac{2}{7} = \frac{6}{7}$	
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	$\frac{1}{5} \times 6 = \frac{6}{5} = 1\frac{1}{5}$ $\frac{2}{5} \times 3 = \frac{6}{5} = 1\frac{1}{5}$	
Multiply mixed numbers by a whole number	I can partition into and	
a whole number	$2\frac{2}{3} \times 3$ $2 \times 3 = 6$ $2 \times 3 = 6$ $2 \times 3 = 6$	
	$2\frac{2}{3} \times 3 = 6 + 2 = 8$	



Progression of skills	Key representations			
Find the whole	If $\frac{1}{\Box}$ is, then the whol	le is ×	If $\Box$ is, then $\frac{1}{\Box}$ is and	d the whole is $ imes$
Children multiply to find the whole from a given part.				
and a great part	$\frac{1}{5}$ of = 6		$\frac{4}{7}$ of = 24	$\frac{1}{7} = 24 \div 4 = 6$
	?	$5 \times 6 = 30$	?	$7 \times 6 = 42$
	6 6 6 6 6	$\frac{1}{5}$ of <b>30</b> = 6	24	$\frac{4}{7}$ of <b>42</b> = 24

# Progression of skills – Division



Year 4	Year 5	Year 6
• Division facts to 12 × 12	Mental strategies	Short division
Divide a number by 1 and itself	<ul> <li>Divide numbers up to 4 digits by a 1-digit number</li> </ul>	<ul><li>Mental strategies</li><li>Long division</li></ul>
Related facts	• Divide by 10, 100 and 1,000	<ul><li>Long division</li><li>Order of operations</li></ul>
<ul> <li>Divide a 2 or 3-digit number</li> <li>by a 1-digit number</li> </ul>	Fraction of an amount	• Divide by 10, 100 and 1,000
Divide by 10 and 100		Divide decimals by integers
		Decimal and fraction equivalents
		Divide a fraction by an integer
		Fraction of an amount
		Calculate percentages
		Calculations involving ratio



Year 5	<ul> <li>Divide numbers mentally drawing upon known facts.</li> <li>Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.</li> <li>Divide whole numbers and those involving decimals by 10, 100 and 1,000</li> </ul>		
Progression of skills	Key representations		
Mental strategies	I can partition into and to help me to divide more easily. $436 \div 4$ $400 \div 4$ $36 \div 4$	I can show groups of on a number line.	To divide by, I can divide by and then divide the result by $436 \div 4 = 436 \div 2 \div 2$ $436 \div 2 = 218$ $218 \div 2 = 109$
Divide numbers up to 4 digits by a 1-digit number  The short division method is introduced for the first time.		reds/tens/ones/ in  2 0 5 r2 3 6 1 7	Th H T O TO



#### **Progression of skills**

#### **Key representations**

#### Divide by 10, 100 and 1,000

Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.

To divide by 10/100/1,000, I move all the digits ... places to the right.

... is one-tenth/one-hundredth/one-thousandth the size of ...

Th	Н	Т	0	Tth	Hth
	•			•	
Th	Н	Т	0	Tth	Hth
				•	
Th	Н	T	0 (	Tth	Hth
			0	00	
Th	Н	Т	0	Tth	Hth

$$120 \div 10 = 12$$

$$120 \div 100 = 1.2$$

$$120 \div 1,000 = 0.12$$

#### Fraction of an amount

Bar models support children to understand that to find a fraction of an amount, we divide by the denominator and multiply by the numerator.

To find  $\models$  of ..., I need to divide by ... and multiply by ...







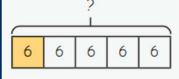
$$\frac{3}{5}$$
 of 20 =



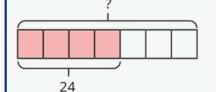
$$\frac{1}{4}$$
 of 84 =

$$\frac{3}{4}$$
 of 84 =

If  $\stackrel{\perp}{=}$  is ..., then the whole is ...  $\times$  ...







$$\frac{4}{7}$$
 of \_\_\_ = 24

Year 4

# Calculation policy

Updated September 2024



#### **Guidance for teachers**

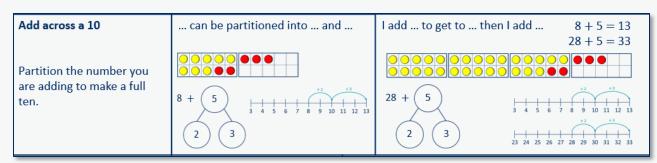


The calculation policy is divided into four sections: addition, subtraction, multiplication and division. At the start of each section, you will find an overview of the progression of skills. Calculations involving decimal numbers and fractions are included.

The calculation policy follows the same concrete, pictorial, abstract approach as our main schemes of learning. Where appropriate, sentence stems and key questions are included alongside the key representations.

Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.



#### **Progression of skills – Addition**



Year 3	Year 4	Year 5
<ul> <li>Add 1s, 10s and 100s to a 3- digit number</li> </ul>	Add 1s, 10s and 100s to a 4- digit number	<ul><li>Add using mental strategies</li><li>Add whole numbers with</li></ul>
<ul><li>Add two numbers (no exchange)</li><li>Add two numbers across a 10</li></ul>	<ul> <li>Add up to two 4-digit numbers</li> <li>Add decimal numbers in the</li> </ul>	<ul><li>more than 4 digits</li><li>Add decimals with up to 2 decimal places</li></ul>
<ul> <li>or 100</li> <li>Complements to 100</li> <li>Add fractions with the same denominator within 1 whole</li> </ul>	<ul> <li>context of money</li> <li>Add fractions and mixed numbers with the same denominator beyond 1 whole</li> </ul>	<ul> <li>Complements to 1</li> <li>Add fractions with denominators that are a multiple of one another</li> </ul>
Calculate the duration of events		



Year 4	<ul> <li>Add numbers with up to 4 digits using a formal written method.</li> <li>Solve simple measure and money problems involving fractions and decimals to 2 decimal places.</li> <li>Add fractions with the same denominator.</li> </ul>	
Progression of skills	Key representations	
Add 1s, 10s and 100s to a 4-digit number  Emphasis on mental strategies including number bonds and related facts.  Prompt children to notice which digit changes.	The ones/tens/hundreds/thousands column will increase by  Thousands Hundreds Tens Ones  Thou	What patterns do you notice? 2,350 + 3 = 2,350 + 30 = 2,350 + 300 = 2,350 + 3,000 = 6,040 + 200 = 6,040 + 500 = 6,040 + 900 = 2,211 + = 2,215 2,211 + = 2,511
Add up to two 4-digit numbers  Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.	do/do not need to make an exchange.	Th H T O  Th H T O  Th H T O  4 6 7 3  + 1 5 1 8  6 1 9 1



Progression of skills	Key representations	
Add decimal numbers in the context of money	pence + pence = pence pounds + pounds = pounds	£3.25 can be partitioned into £3 + 20p + 5p
Emphasis on partitioning and use of number lines rather than formal written calculations.	45p + 25p = 70p £2 + £3 = £5 £5 + 70p = £5.70	£2.45 £5.45 £5.65 £5.70
Add fractions and mixed numbers with the same denominator beyond 1 whole	When adding fractions with the same den fifths $+$ fifths $=$ fifths $\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1\frac{2}{5}$	ominator, I only add the numerator. $\frac{+\frac{3}{5}}{0}$

#### **Progression of skills - Subtraction**



Year 3	Year 4	Year 5
Subtract 1s, 10s and 100s     from a 3-digit number	Subtract 1s, 10s, 100s and 1,000s from a 4-digit number	Subtract whole numbers with more than 4 digits
Subtract two numbers (no exchange)	Subtract up to two 4-digit numbers	Subtract using mental strategies
Subtract two numbers across     a 10 or 100	Subtract decimal numbers in the context of money	Subtract decimals with up to 2 decimal places
Complements to 100	Subtract fractions and mixed	Complements to 1
Subtract fractions with the same denominator within 1 whole	numbers with the same denominator	Subtract fractions with denominators that are a multiple of one another



Year 4	<ul> <li>Subtract numbers with up to 4 digits using a formal written method.</li> <li>Solve simple measure and money problems involving fractions and decimals to 2 decimal places.</li> <li>Subtract fractions with the same denominator.</li> </ul>	
Progression of skills	Key representations	
Subtract 1s, 10s, 100s and 1,000s from a 4-digit number  Emphasis on mental strategies including number bonds and related facts.  Prompt children to notice which digit changes.	The ones/tens/hundreds/thousands column will decrease by  Thousands Hundreds Tens Ones  Thousands Hundreds Tens Ones  3,425 - 2 = 3,425 - 200 = 3,425 - 2,000 =	What patterns do you notice? 4,356 - 3 = 4,356 - 30 = 4,356 - 300 = 4,356 - 3,000 = 6,940 - 200 = 6,940 - 300 = 6,940 - 300 = 6,940 - 400 = 4,433 - 4,433 -
Subtract up to two 4-digit numbers  Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.	I need to subtract ones/tens/hundreds. I do  I can exchange 1 for 10	Н Т О



Progression of skills	Key representations	
Subtract decimal numbers in the context of money	I can partition £ into £ and 100p $f f = f$ $100pp =p$	£3.26 can be partitioned into £3 + 20p + 6p
Emphasis here is on partitioning and use of number lines rather than formal written calculations.	£5 - £3.26 £4 - £3 = £1 100p - 26p = 74p £5 - £3.26 = £1.74	- 6p - 20p - £3 £1.74 £1.80 £2 £5
Subtract fractions and mixed numbers with the same denominator  Include subtracting fractions from wholes.	When subtracting fractions with the same de I only subtract the numerator tenths — tenths	nominator, 2 5 6
from wholes.	$\frac{16}{10} - \frac{5}{10}$ $\frac{16}{10} - \frac{9}{10}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

#### **Progression of skills – Multiplication**



Year 3	Year 4	Year 5
The 3 times-table	• Times-table facts to $12 \times 12$	Multiples and factors
The 4 times-table	Multiply by 1 and 0	Square and cube numbers
The 8 times-table	Multiply 3 numbers	Multiply numbers up to 4
Related facts	Factor pairs	digits by a 1-digit number
<ul> <li>Multiply a 2-digit number by a 1-digit number - no exchange</li> </ul>	Multiply by 10 and 100	Multiply numbers up to 4  digits by a 2 digit number.
<ul> <li>Multiply a 2-digit number by a</li> </ul>	<ul><li>Related facts</li></ul>	digits by a 2-digit number
1-digit number - with		Multiply by 10, 100 and 1,000
exchange	Mental strategies	Mental strategies
Scaling	Multiply a 2 or 3-digit number     Let a 1 digit number	Multiply fractions by a whole
Correspondence problems	by a 1-digit number	number
	Scaling	Multiply mixed numbers by a
	Correspondence problems	whole number
		Find the whole



Year 4	<ul> <li>Recall multiplication facts for multiplication tables up to 12 × 12</li> <li>Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers.</li> <li>Recognise and use factor pairs and commutativity in mental calculations.</li> <li>Multiply two-digit and three-digit numbers by a one-digit number using formal written layout.</li> <li>Solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.</li> </ul>	
Progression of skills	Key representations	
Times-table facts to 12 × 12  Encourage daily counting in multiples both forwards and back. Encourage children to notice links between related times-tables.	groups of = times is equal to × =    1   2   3   4   5   6   7   8   9   10     11   12   13   14   15   16   17   18   19   20     21   22   23   24   25   26   27   28   29   30     31   32   33   34   35   36   37   38   39   40     41   42   43   44   45   46   47   48   49   50     51   52   53   54   55   56   57   58   59   60     61   62   63   64   65   66   67   68   69   70     71   72   73   74   75   76   77   78   79   80     81   82   83   84   85   86   87   88   89   90     91   92   93   94   95   96   97   98   99   100     71   72   73   74   75   76   77   78   78   79   80     72   73   74   75   76   77   78   79   80     74   75   76   77   78   79   80     75   75   75   75   77   78   79   80     76   77   78   79   79   79   79   79   79	
Multiply by 1 and 0	Any number multiplied by 1 is equal to  Any number multiplied by 0 is equal to $1 \times 1 = 1$ $2 \times 1 = 2$ $2 \times 0 = 0$ $3 \times 1 = 3$ $3 \times 0 = 0$ $4 \times 1 = 4$ $4 \times 0 = 0$	



Progression of skills	Key representations
Multiply 3 numbers  Children use their understanding of commutativity to multiply more efficiently.	To work out $\times$ , I can first calculate $\times$ and then multiply the answer by $4 \times 2 \times 3 = 8 \times 3 = 24$ $2 \times 3 \times 4 = 6 \times 4 = 24$ $3 \times 4 \times 2 = 12 \times 2 = 24$
Factor pairs  Children explore equivalent calculations using different factors pairs.	$12 = \times, \text{ so } \times 12 = \times \times$ $8 \times 6 = 8 \times 3 \times 2$ $8 \times 6 = 24 \times 2$ $6 \times 8 = 6 \times 4 \times 2$ $6 \times 8 = 24 \times 2$
Multiply by 10 and 100  Some children may overgeneralise that multiplying by 10 or 100 always results in adding zeros. This will cause issues later when multiplying decimals.	When I multiply by 10, the digits move place value column to the left is 10 times the size of  H T 0  35 $\times$ 10 = 350  When I multiply by 100, the digits move place value columns to the left is 100 times the size of  Th H T 0  35 $\times$ 10 = 350



Progression of skills	Key representations	
Related facts  Use knowledge of multiplying by 10 and 100	$\dots \times \dots$ ones is equal to $\dots$ ones so $\dots \times \dots$ tens is equal to $\dots$ tens and $\dots \times \dots$ hundreds is equal to $\dots$ hundreds.	
to scale times-table facts.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
Mental strategies	tens multiplied by is equal to tensones multiplied by is equal to ones.	
Partition 2 or 3-digit numbers to multiply using informal methods.	Tens Ones  26  20  6  20  3 × 26 = 60 + 18 = 78  60  10 × 8 = 80  10 × 8 = 80  10 × 8 = 80  26 × 8 = 80 + 80 + 48 = 208	



Progression of skills	Key representations				
Multiply a 2 or 3-digit number by a 1-digit number	To multiply a 2-digit number by, I mult To multiply a 3-digit number by, I mult hundreds by	• •	s by , the t	ens by and	d the
The short multiplication method is introduced for the first time, initially in an expanded form.	T 0 H T 0 3 4 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		H T O 3 4 5 1 7 O 1 2		
Scaling	is times the size of				
Children focus on multiplication as scaling ( times the size).	7 7 7 7 7 7 7 7 A Computer mouse costs £7 A keyboard costs 6 times as much.  A computer mouse costs £7 A yellow ribbon is 7 times as long.				
Correspondence problems	For every, there are possibilities.				
	There are × possibilities altogether.		Deep pan	Italian	Thin
Encourage children to use	·	Cheese	C DP	CI	C Th
tables to show all the	A pizza company offers a choice	Mushroom	M DP	ΜI	M Th
different possible	of 5 toppings and 3 bases.	Vegetable	V DP	VI	V Th
combinations.		Chicken	C DP	СІ	C Th
	$5 \times 3 = 15$	Tuna	T DP	TI	T Th

## Progression of skills – Division



Year 3	Year 4	Year 5
Divide by 3	• Division facts to $12 \times 12$	Mental strategies
Divide by 4	Divide a number by 1 and	Divide numbers up to 4 digits
Divide by 8	itself	by a 1-digit number
Related facts	Related facts	<ul> <li>Divide by 10, 100 and 1,000</li> </ul>
Divide a 2-digit number by a     1-digit number - no exchange	Divide a 2 or 3-digit number by a 1-digit number	Fraction of an amount
<ul> <li>Divide a 2-digit number by a 1-digit number - with remainders</li> </ul>	Divide by 10 and 100	
<ul> <li>Unit fractions of a set of objects</li> </ul>		
Non-unit fractions of a set of objects		



Year 4	<ul> <li>Recall division facts for multiplication tables up to 12 × 12</li> <li>Use place value, known and derived facts to divide mentally, including: dividing by 1</li> <li>Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths.</li> </ul>		
Progression of skills	Key representations		
<b>Division facts to 12 × 12</b> Encourage children to	There are groups of in ÷ =	has been shared equally into equal groups $\div$ =	
compare the grouping and sharing structures of division and to make links with times-table facts.	$2 \times 6 = 12 \\ 12 \div 6 = 2$ 0 6 12	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
Divide a number by 1 and itself	When I divide a number by 1, the number remains the same.	When I divide a number by itself, the answer is 1 5 shared between 5 is 1	
Children may try to divide a number by zero and it should be highlighted that this is not possible.	5 shared between 1 is 5  There are <b>5</b> groups of 1 in 5	There is 1 group of 5 in 5	



Progression of skills	Key representations	
Related facts  Link to known times-table facts.		ndreds.
Divide a 2 or 3-digit number by a 1-digit number  Progress from divisions with no exchange, to divisions with exchange and then divisions with remainders.	and ones. $80 \div 4 = 20$ $4 \div 4 = 1$	



Progression of skills	Key representations		
Divide by 10 and 100  Encourage children to	When I divide by 10, the digits move 1 place value column to the right is one-tenth the size of	When I divide by 100, the digits move 2 place value columns to the right is one-hundredth the size of	
notice that dividing by 100 is the same as dividing by 10 twice.	O Tth Hth  T O Tth Hth	O Tth Hth  T O Tth Hth	
	O Tth Hth T O Tth Hth	O Tth Hth T O Tth Hth	
	$2 \div 10 = 0.2$ $12 \div 10 = 1.2$	$2 \div 100 = 0.02$ $12 \div 100 = 0.12$	

Year 3

# Calculation policy

Updated September 2024



#### **Guidance for teachers**

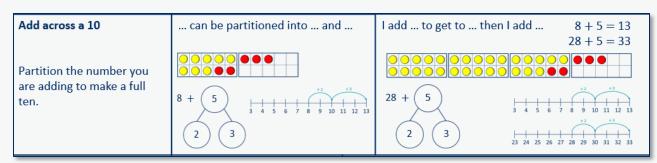


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Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.



# Progression of skills – Addition



Year 2	Year 3	Year 4
Add 1s to any number (related facts)	Add 1s, 10s and 100s to a 3- digit number	Add 1s, 10s and 100s to a 4- digit number
Add three 1-digit numbers	<ul> <li>Add two numbers (no exchange)</li> </ul>	Add up to two 4-digit numbers
Add across a 10		
Add multiples of 10	<ul> <li>Add two numbers across a 10 or 100</li> </ul>	<ul> <li>Add decimal numbers in the context of money</li> </ul>
Add 10s to any number	Complements to 100	Add fractions and mixed
<ul> <li>Add two 2-digit numbers (not across a ten)</li> </ul>	Add fractions with the same denominator within 1 whole	numbers with the same denominator beyond 1 whole
<ul> <li>Add two 2-digit numbers (across a ten)</li> </ul>	Calculate the duration of events	
Missing numbers		



Year 3	<ul> <li>Add numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds.</li> <li>Add numbers with up to three digits, using formal written methods of columnar addition.</li> <li>Add fractions with the same denominator within 1 whole.</li> <li>Calculate the time taken by particular events or tasks.</li> </ul>		
Progression of skills	Key representations		
Add 1s, 10s or 100s to a	The ones/tens/hundreds colu	mn will increase by	What patterns do you notice?
3-digit number  Emphasis on mental strategies including number bonds and related facts.  Prompt children to notice which digit changes.	Hundreds Tens Ones  444 + 5 =  444 + 50 =  444 + 500 =	H T O  W W D O O O O  W W D O O O O  W TO O O O O O  TO O O O O O O  TO O O O	235 + 3 =  235 + 30 =  235 + 300 =  111 +
Add two numbers	ones + ones = ones		?
(no exchange)	tens + tens = tens hundreds + hundreds		
Mental strategies and introduction of formal written method.		Hundreds	Tens Ones  10 10 10 10 10 10 10 10 10 10 10 10 10 1



Progression of skills	Key representations	
Add two numbers across a 10 or 100  Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.	There are ones, so I do/do not need to read the read of the re	Part of the state
Complements to 100  Pairs of numbers which total 100	plus is equal to 100  38  100  38  ?	I add to get to the next 10, then to get to 100 $ 38 + 62 = 100 $ $ 62 + 38 = 100 $ $ 100 = 38 + 62 $ $ 100 = 62 + 38 $



Progression of skills	Key representations
Add fractions with the same denominator within 1 whole  Make links with known facts.	When adding fractions with the same denominator, I only add the numerator fifths $+$ fifths $=$ fifths $\frac{1}{5} + \frac{1}{5}$ $\frac{1}{5} + \frac{2}{5}$ $\frac{1}{5} + \frac{3}{5}$
Calculate the duration of events  Find durations of time between a given start and end point. Children will need to calculate complements to 60	From to o'clock is minutes. From o'clock to is minutes. The total time taken is minutes.  H:25 4:55  Start finish  Y:25 4:55  2:25 3:00 3:18

#### **Progression of skills - Subtraction**



Year 2	Year 3	Year 4
<ul> <li>Subtract 1s from any number (related facts)</li> </ul>	Subtract 1s, 10s and 100s     from a 3-digit number	Subtract 1s, 10s, 100s and 1,000s from a 4-digit number
<ul><li>Subtract across a 10</li><li>Subtract multiples of 10</li></ul>	Subtract two numbers (no exchange)	Subtract up to two 4-digit numbers
Subtract multiples of 10     Subtract 10s from any number	Subtract two numbers across     a 10 or 100	Subtract decimal numbers in the context of money
<ul> <li>Subtract two 2-digit numbers (not across a ten)</li> </ul>	Complements to 100	Subtract fractions and mixed numbers with the same
<ul> <li>Subtract two 2-digit numbers (across a ten)</li> </ul>	<ul> <li>Subtract fractions with the same denominator within 1 whole</li> </ul>	denominator
Missing numbers		



Year 3	<ul> <li>Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds.</li> <li>Subtract numbers with up to three digits, using formal written methods.</li> <li>Subtract fractions with the same denominator within 1 whole.</li> </ul>			
Progression of skills	Key representations			
Subtract 1s, 10s and 100s from a 3-digit number  Emphasis on mental strategies including number bonds and related facts.  Prompt children to notice which digit changes.	The ones/tens/hundreds column will decrease by  Hundreds Tens Ones H T O			
Subtract two numbers (no exchange)  Mental strategies and introduction of formal written method.	ones — ones = ones tens — tens = tens hundreds — hundreds  Hundreds Tens Ones  769  147 ?  143			



Progression of skills	Key representations	
Subtract two numbers across a 10 or 100  Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.	I need to subtract ones. I do/do not need to I need to subtract tens. I do/do not need to I can exchange 1 for 10  Tens  Tens  Ones  1 8	_
Complements to 100	100 minus is equal to	I subtract tens, then I subtract ones.
Focus on subtraction facts.  Encourage children to notice patterns.	100 38 100 38 ?	



Progression of skills	Key representations
Subtract fractions with the same denominator within 1 whole	When subtracting fractions with the same denominator, I only subtract the numerator fifths $-$ fifths $=$ fifths $\frac{5}{5} - \frac{1}{5}$
Make links with known facts.	$\frac{4}{5} - \frac{1}{5}$
	$\frac{3}{5} - \frac{1}{5}$

#### **Progression of skills – Multiplication**



Year 2	Year 3	Year 4
Link repeated addition and	The 3 times-table	• Times-table facts to $12 \times 12$
multiplication	The 4 times-table	Multiply by 1 and 0
Use arrays	The 8 times-table	Multiply 3 numbers
Double	Related facts	Factor pairs
The 2 times-table	<ul> <li>Multiply a 2-digit number by a</li> </ul>	Multiply by 10 and 100
The 10 times-table	1-digit number - no exchange	Related facts
The 5 times-table	Multiply a 2-digit number by a	<ul> <li>Mental strategies</li> </ul>
Missing numbers	1-digit number - with exchange	<ul> <li>Multiply a 2 or 3-digit number</li> </ul>
	<ul> <li>Scaling</li> </ul>	by a 1-digit number
	<ul> <li>Correspondence problems</li> </ul>	Scaling
		Correspondence problems



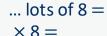
Year 3	<ul> <li>Recall and use multiplication facts for the 3, 4 and 8 multiplication tables.</li> <li>Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.</li> <li>Solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.</li> </ul>			
Progression of skills	Key representations			
The 3 times-table	groups of 3 =	times 3 is equal to		
Encourage daily counting in multiples both forwards and back.	× 3 = 3, times = 3 × =	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
	3 3 3	0 3 6 9 12 15 18 21 24 27 30 33 36		
The 4 times-table	groups of 4 =	times 4 is equal to		
Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2 and 4 times-tables.	× 4 = 4, times = 4 × = 4 4 4	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		



#### **Progression of skills**

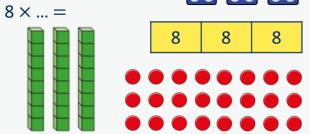
#### The 8 times-table

Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2, 4 and 8 times-tables.



**Key representations** 

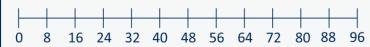
8, ... times =



... times 8 is equal to ...

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30

$$3 \times 8 = 24$$
  $24 = 3 \times 8$ 



#### **Related facts**

Use knowledge of multiplying by 10 to scale times-table facts.

 $\dots \times \dots$  ones is equal to  $\dots$  ones

so ... × ... tens is equal to ... tens.











$$3\times 4=12$$

$$3 \times 40 = 120$$

# Multiply a 2-digit number by a 1-digit number - no exchange

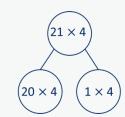
Children apply their understanding of partitioning to represent and solve calculations using the expanded method.

- ... tens multiplied by ... is equal to ... tens.
- ...ones multiplied by ... is equal to ... ones.

Tens	Ones
	••
	••

$$30 \times 2 = 60$$
$$2 \times 2 = 4$$

$$32 \times 2 = 64$$



Tens	Ones
000	1
000	1
000	1
000	1



Progression of skills	Key representations				
Multiply a 2-digit number by a 1-digit number - with exchange  Children apply their understanding of partitioning to represent and solve calculations using the expanded method.	tens multiplied by is equal to tens ones multiplied by is equal to ones.	45 × 3  Tens Ones  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0			
Scaling  Children focus on multiplication as scaling ( times the size) as opposed to repeated addition.	There are times as many as  2  \( \triangle	is times the size of is times the length/height of  4 cm  16 cm  Miss Smith is twice the height of Jo.			



Progression of skills	Key representations				
Correspondence problems (How many ways?)	For every , there are possible There are × possibilities altogether.				
		hats	scarves		
Encourage children to work systematically to find all the		blue 🌲	ALD!	For every hat, there are two possible	
different possible combinations.		orange 🎘	SIE SIE	scarves. $3 \times 2 = 6$	
		purple 🎘		There are 6 possibilities altogether.	

### Progression of skills – Division



Year 2	Year 3	Year 4
Divide by 2	Divide by 3	• Division facts to $12 \times 12$
Divide by 10	Divide by 4	Divide a number by 1 and
Divide by 5	Divide by 8	itself
Missing numbers	Related facts	Related facts
Unit fractions	Divide a 2-digit number by a	Divide a 2 or 3-digit number
Non-unit fractions	1-digit number - no exchange	by a 1-digit number
	<ul> <li>Divide a 2-digit number by a 1-digit number - with remainders</li> </ul>	Divide by 10 and 100
	<ul> <li>Unit fractions of a set of objects</li> </ul>	
	<ul> <li>Non-unit fractions of a set of objects</li> </ul>	



Year 3	<ul> <li>Recall and use division facts for the 3, 4 and 8 multiplication tables.</li> <li>Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.</li> <li>Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators.</li> </ul>		
Progression of skills	Key representations		
Divide by 3  Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are groups of 3 in $ \div 3 =$ $2 \times 3 = 6$ $6 \div 3 = 2$	has been shared equally into 3 equal groups. $\div$ 3 = $2 \times 3 = 6$ $6 \div 3 = 2$	
Divide by 4  Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are groups of 4 in $\div$ 4 = $2 \times 4 = 8$ $8 \div 4 = 2$	has been shared equally into 4 equal groups. $\div$ 4 = $2 \times 4 = 8$ $8 \div 4 = 2$	



#### **Progression of skills**

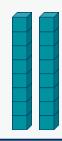
#### **Key representations**

#### Divide by 8

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.

There are ... groups of 8 in ...

$$... \div 8 =$$



$$2 \times 8 = 16$$
  
 $16 \div 8 = 2$ 



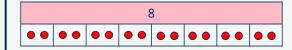


... has been shared equally into 8 equal groups.

$$... \div 8 =$$







$$2 \times 8 = 16$$
  
 $16 \div 8 = 2$ 

#### **Related facts**

Link to known times-table facts.

 $\dots \div \dots$  is equal to ...,

so ... tens ÷ ... is equal to ... tens.











$$12 \div 3 = 4$$
  
 $120 \div 3 = 40$ 

# Divide a 2-digit number by a 1-digit number - no exchange

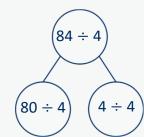
Partition into tens and ones to divide and then recombine.

- ... tens divided by ... is equal to ... tens.
- ... ones divided by ... is equal to ... ones.

Tens	Ones
	••
	••

$$60 \div 2 = 30$$
  
 $4 \div 2 = 2$ 

$$64 \div 2 = 32$$



Tens	Ones
000	0
0000	0
000	0
000	0



#### **Progression of skills Key representations** Divide a 2-digit number by ... tens divided by ... is equal to ... tens. There are ... groups of ... a 1-digit number - with ... ones divided by ... is equal to ... ones. There are ... remaining. remainders $31 \div 4 = 7 \text{ r}$ 3 Encourage children to partition numbers flexibly Tens Ones (96 ÷ 4 to help them to divide more \_\_\_\_\_ efficiently. $94 \div 4 = 23 \text{ r}$ 2 80 ÷ 4 $(16 \div 4)$ \_\_\_\_ Tens Ones Ones Tens 00 000 $80 \div 4 = 20$ 00 00 $16 \div 4 = 4$ 00 00 $96 \div 4 = 24$ 00 Unit fractions of a set of One ... of ... is ... The whole is divided into ... equal parts. objects Each part is $\frac{1}{\Box}$ of the whole. $\frac{1}{4}$ of 12 is 3 Bar models are useful to show the link between $\frac{1}{3}$ of 36 is 12 division and fractions, for example, dividing by 3 and finding a third. $\frac{1}{4}$ of 12 apples is 3 apples.



Progression of skills	Key representations		
Non-unit fractions of a set of objects	The whole is divided into equal parts. Each part is $\frac{1}{\Box}$ of the whole.	$\frac{1}{\Box}$ of is, so $\frac{\Box}{\Box}$ of is	
Bar models are a useful representation and show the links with division and		$\frac{3}{4}$ of 12 is 9	
multiplication.	$\frac{3}{4}$ of 12 apples is 9 apples.	$\frac{2}{3}$ of 36 is 24	

Year 2

# Calculation policy

Updated September 2024



#### **Guidance for teachers**

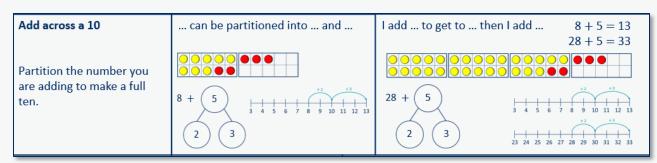


The calculation policy is divided into four sections: addition, subtraction, multiplication and division. At the start of each section, you will find an overview of the progression of skills. Calculations involving decimal numbers and fractions are included.

The calculation policy follows the same concrete, pictorial, abstract approach as our main schemes of learning. Where appropriate, sentence stems and key questions are included alongside the key representations.

Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.



## Progression of skills – Addition



Year 1	Year 2	Year 3
Add together	<ul> <li>Add 1s to any number (related facts)</li> </ul>	Add 1s, 10s and 100s to a 3- digit number
Add more	<ul> <li>Add three 1-digit numbers</li> </ul>	Add two numbers (no
Bonds within 10	Add timee 1-digit numbers     Add across a 10	exchange)
Related facts within 20	<ul> <li>Add across a 10</li> <li>Add multiples of 10</li> </ul>	Add two numbers across a 10
Missing numbers	·	or 100
	Add 103 to any namber	Complements to 100
	<ul> <li>Add two 2-digit numbers (not across a ten)</li> </ul>	<ul> <li>Add fractions with the same denominator within 1 whole</li> </ul>
	<ul> <li>Add two 2-digit numbers (across a ten)</li> </ul>	Calculate the duration of events
	Missing numbers	



Year 2	<ul> <li>Recall and use addition facts to 20 fluently, and derive and use related facts up to 100</li> <li>Add numbers using concrete objects, pictorial representations, and mentally, including:         <ul> <li>a two-digit number and 1s</li> <li>a two-digit number and 10s</li> <li>2 two-digit numbers</li> <li>adding 3 one-digit numbers</li> </ul> </li> <li>Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.</li> </ul>			
Progression of skills	Key representations			
Add ones to any number (related facts)  Make links to known facts.	I know that and = so and =	What do you notice? Can you continue the pattern? 5+2=7 $15+2=17$ $25+2=27$		
Add three 1-digit numbers  Prompt children to understand that addition can be done in any order and to make links to known facts.	and are a bond to 10  10 + =  8 9 1	Pouble + =	What do you notice? Which addition is the easiest to calculate? $8+9+1=\\8+1+9=\\9+1+8=$	



Progression of skills	Key representations				
Add across a 10	can be partitioned into and		I add to get to th	en I add	8 + 5 = 13 28 + 5 = 33
Partition the number being added to make a full ten.					
	8 + 5		28 + 5	3 4 5 6 7	7 8 9 10 11 12 13
			2 3	23 24 25 26 2	7 28 29 30 31 32 33
Add multiples of 10	so tens + tens = tens  What is $3 + 2 = 5$ $30 + 20 = 50$		t is the same?	2	20
Make links to known facts within ten.			t is different?	2	30
Add 10s to any number			ld I need to add 10	1 kp ow that	and =
Add 103 to any number	tens + tens = tens tens and ones =	tin		so and =	
Make links to known facts.	1 1 2 3 4 5		2 3 4 5 6 7 8 9 10 12 13 14 15 16 17 18 19 20 22 23 24 25 26 27 28 29 30 32 33 34 35 36 37 38 39 40 42 43 44 45 46 47 48 49 50 52 53 54 55 56 57 58 59 60		- 20 = 50 - 20 = 54



Progression of skills	Key representations		
Add 2-digit numbers (not across a ten)  Lining up ones and tens in columns will support with later written methods.	ones + ones = ones tens + tens = tens	Tens Ones	3 ones + 1 one = 4 ones 4 tens + 2 tens = 6 tens 6 tens + 4 ones = 64 21  ?  43  21
Add 2-digit numbers (across a ten)  Begin to exchange 10 ones for 1 ten.	There are ones, so I do/do ones = ten and ones	12 ones = 4 tens + 3	
Missing numbers  Solve missing number problems and use the inverse to check.	How many more do you need to make? $6 +  = 10$ $10 -  = 6$	If is a whole and is a part, then is the other part.	can be partitioned into and $10+8=12+ \hfill 10+8=12+ \hfill 10+8$

### **Progression of skills - Subtraction**



Year 1	Year 2	Year 3
<ul><li>Find a part</li><li>Take away</li></ul>	Subtract 1s from any number (related facts)	Subtract 1s, 10s and 100s     from a 3-digit number
Bonds within 10	<ul><li>Subtract across a 10</li><li>Subtract multiples of 10</li></ul>	<ul> <li>Subtract two numbers (no exchange)</li> </ul>
<ul><li>Related facts within 20</li><li>Missing numbers</li></ul>	Subtract 10s from any number	Subtract two numbers across a 10 or 100
	<ul> <li>Subtract two 2-digit numbers (not across a ten)</li> </ul>	Complements to 100
	Subtract two 2-digit numbers (across a ten)	<ul> <li>Subtract fractions with the same denominator within 1 whole</li> </ul>
	Missing numbers	



•	Recall and use subtraction facts to 20 fluently, and derive and use related facts up to
	100

- Subtract numbers using concrete objects, pictorial representations, and mentally, including:
  - a two-digit number and 1s
  - a two-digit number and 10s
  - 2 two-digit numbers
- Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.

#### **Progression of skills**

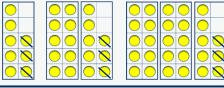
#### **Key representations**

# Subtract ones from any number

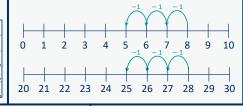
(related facts)

Make links to known facts.

I know that ... minus ... = ... so ... minus ... = ...



... less than ... is ... so ... less than ... is ...



What do you notice? Can you continue the pattern?

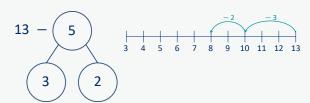
$$8-3=5$$
  
 $18-3=15$   
 $28-3=25...$ 

#### **Subtract across a 10**

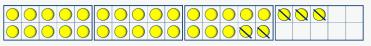
Partition the number being subtracted to bridge through a ten.

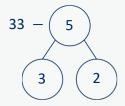
... can be partitioned into ... and ...

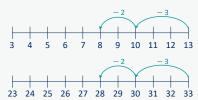




Make links with related facts.









Progression of skills	Key representations		
Subtract multiples of 10  Make links to known facts within ten.	what is the same? What is different? $5 - 2 = 3$ $5 - 2 = 3$ $50 - 20 = 30$ What is the same? $5 - 2 = 3$ $0 = 10 \text{ 20} \text{ 30} \text{ 40} \text{ 50} \text{ 60} \text{ 70} \text{ 80} \text{ 90} \text{ 100}$ $0 = 10 \text{ 20} \text{ 30} \text{ 40} \text{ 50} \text{ 60} \text{ 70} \text{ 80} \text{ 90} \text{ 100}$		2 20 10 5 2 ? 50
Subtract 10s from any number  Make links to known facts.	tens — tens = tens tens and ones =	To subtract I need to subtract 10 times.    1   2   3   4   5   6   7   8   9   10     11   12   13   14   15   16   17   18   19   20     21   22   23   24   25   26   27   28   29   30     31   32   33   34   35   36   37   38   39   40     41   42   43   44   45   46   47   48   49   50     51   52   53   54   55   56   57   58   59   60	I know that minus = so minus = $50 - 20 = 30$ $54 - 20 = 34$



Progression of skills	Key representations		
Subtract two 2-digit numbers (not across a ten)	ones – ones = ones tens – tens = tens		= 2 tens
Subtract two 2-digit numbers (across a ten)  Begin to exchange 1 ten for 10 ones.	43 T T T T T T T T T T T T T T T T T T T	ecause I do not have enough or  - 5 ones to exchange 1 ten for 10 ones)	T O
Missing numbers  Solve missing number problems and use the inverse to check.	How many do you need to subtract to make? $10 - \square = 6$ $6 + \square = 10$	If is a whole and is a part, then is the other part. $7 - 3 = \boxed{}$ $\boxed{} + 3 = 7$	can be partitioned into and $18 - \boxed{} = 12 + 2$

### **Progression of skills – Multiplication**



Year 1	Year 2	Year 3
<ul> <li>Count in 2s, 5s and 10s</li> <li>Add equal groups</li> <li>Make arrays</li> <li>Make doubles</li> </ul>	<ul> <li>Link repeated addition and multiplication</li> <li>Use arrays</li> <li>Double</li> <li>The 2 times-table</li> </ul>	<ul> <li>The 3 times-table</li> <li>The 4 times-table</li> <li>The 8 times-table</li> <li>Related facts</li> </ul>
	<ul> <li>The 10 times-table</li> <li>The 5 times-table</li> <li>Missing numbers</li> </ul>	<ul> <li>Multiply a 2-digit number by a 1-digit number - no exchange</li> <li>Multiply a 2-digit number by a 1-digit number - with exchange</li> <li>Scaling</li> </ul>
		Correspondence problems



Year 2	<ul> <li>Recall and use multiplication facts for the 2, 5 and 10 multiplication tables.</li> <li>Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (×) and equals (=) signs.</li> <li>Show that multiplication of two numbers can be done in any order (commutative).</li> </ul>		
Progression of skills	Key representations		
Link repeated addition and multiplication  Encourage children to make the link between repeated addition and multiplication.	There are equal groups with in each ground there are altogether.	3 + 3 = 6 3   3   2 × 3 = 6 20   5 + 5 + 5 + 5 = 20	
Use arrays	There are rows with in each row.		
Encourage children to see that multiplication is commutative.	There are columns with in each column.  3 lots of $5 = 15$ 5 + 5 + 5 = 15 5 lots of $3 = 15$ 3 + 3 + 3 + 3 + 3 =	$3 \times 5 = 15$ $5 \times 3 = 15$ $3 \times 5 = 5 \times 3$	
Double  Encourage children to make links with related facts.	Double is  Double $4 = 4 + 4$ Double 4 is 8	Double is so double is  Double 4 is 8  Double 40 is 80	



Progression of skills	Key representations	
The 2 times-table  Encourage daily counting in multiples both forwards and back. Notice that all multiples of 2 are even numbers.	lots of 2 = × 2 =	times 2 is equal to $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
	2 2 2 2	0 2 4 6 8 10 12 14 16 18 20 22 24
The 10 times-table  Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.	lots of 10 = ×	times 10 is equal to $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$



Progression of skills	Key representations		
The 5 times-table  Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.	lots of 5 = × 5 =	times 5 is equal to $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	? 5 5 5 5 5	0     5     10     15     20     25     30     35     40     45     50     55     60	
Missing numbers	is equal to groups of	times is equal to	
Make links to known facts.	18 socks, how many pairs?		
	0 2 4 6 8 10 12 14 16 18 20	18 = 2 ×	

# Progression of skills – Division



Year 1	Year 2	Year 3
Make equal groups – grouping	Divide by 2	Divide by 3
Make equal groups – sharing	Divide by 10	Divide by 4
Find a half	Divide by 5	Divide by 8
Find a quarter	Missing numbers	Related facts
	Unit fractions	Divide a 2-digit number by a
	Non-unit fractions	1-digit number - no exchange
		<ul> <li>Divide a 2-digit number by a 1-digit number - with remainders</li> </ul>
		<ul> <li>Unit fractions of a set of objects</li> </ul>
		<ul> <li>Non-unit fractions of a set of objects</li> </ul>



Year 2	<ul> <li>Recall and use division facts for the 2, 5 and 10 multiplication tables.</li> <li>Calculate mathematical statements for division within the multiplication tables and write them using the division (÷) and equals (=) signs.</li> <li>Recognise, find, name and write fractions <sup>1</sup>/<sub>3</sub>, <sup>1</sup>/<sub>4</sub>, <sup>2</sup>/<sub>4</sub> and <sup>3</sup>/<sub>4</sub> of a quantity.</li> </ul>		
Progression of skills	Key representations		
Divide by 2  Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts and halving.	There are equal groups of 2 $\div$ 2 = $4 \times 2 = 8$ $8 \div 2 = 4$ $0 \cdot 1$ $2 \cdot 3$ $4 \cdot 5$ $6 \cdot 7$ $8 \cdot 9$ $10$	shared equally between 2 is Half of is $\div$ 2 = $4 \times 2 = 8$ $8 \div 2 = 4$	
Divide by 10  Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are equal groups of 10 $\div$ 10 = $6 \times 10 = 60$ $60 \div 10 = 6$	shared equally between 10 is $ \div 10 = \\ 6 \times 10 = 60 \\ 60 \div 10 = 6 $	



Progression of skills	Key representations	
Divide by 5  Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.	There are equal groups of 5 $\div$ 5 = $\div$ 6 × 5 = 30 × 5 = 6 × 5 = 3	
Missing numbers  Bar models are useful to show the link between multiplication and division.	divided by 2/5/10 is equal to	☐ · 10 – 10



Progression of skills	Key representations			
Unit fractions  In Y2 the focus is on finding $\frac{1}{2}$ , $\frac{1}{4}$ and $\frac{1}{3}$	The objects have been shared fairly into groups.  1 of is	There are equal parts.  There is part circled. $\frac{1}{\Box}$ is circled.		
Bar models are useful to show the link between division and finding a fraction.				
Non-unit fractions	The objects have been shared fairly into groups.	There are equal parts. There are parts circled.		
In Y2 the focus is on finding $\frac{2}{4}$ and $\frac{3}{4}$	of is	is circled.		
Prompt children to notice that $\frac{2}{4}$ is equivalent to $\frac{1}{2}$				

Year 1

# Calculation policy

Updated September 2024



#### **Guidance for teachers**

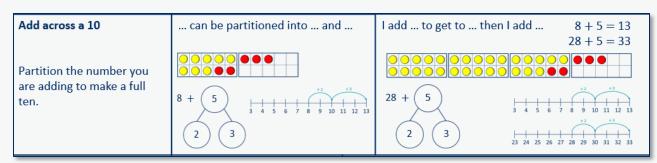


The calculation policy is divided into four sections: addition, subtraction, multiplication and division. At the start of each section, you will find an overview of the progression of skills. Calculations involving decimal numbers and fractions are included.

The calculation policy follows the same concrete, pictorial, abstract approach as our main schemes of learning. Where appropriate, sentence stems and key questions are included alongside the key representations.

Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.



## Progression of skills – Addition



Reception	Year 1	Year 2
<ul> <li>Conceptually subitise to 5</li> <li>1 more</li> <li>Notice the composition of numbers within 10</li> <li>Combine 2 groups</li> <li>Add more</li> </ul>	<ul> <li>Add together</li> <li>Add more</li> <li>Bonds within 10</li> <li>Related facts within 20</li> <li>Missing numbers</li> </ul>	<ul> <li>Add 1s to any number (related facts)</li> <li>Add three 1-digit numbers</li> <li>Add across a 10</li> <li>Add multiples of 10</li> <li>Add 10s to any number</li> <li>Add two 2-digit numbers (not across a ten)</li> <li>Add two 2-digit numbers (across a ten)</li> <li>Missing numbers</li> </ul>



Year 1  Progression of skills	<ul> <li>Read, write and interpret mathematical statements involving addition (+) and equals (=) signs.</li> <li>Represent and use number bonds within 20</li> <li>Add 1-digit and 2-digit numbers to 20, including zero.</li> <li>Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as 7 =  + 2</li> <li>Key representations</li> </ul>		
Add together	There are	is a part.	plus is equal to
(aggregation)	There are	is a part.	is equal to +
	There are altogether.	is the whole.	
2 quantities are combined to find the total.		4 2	4 + 2 = 6 $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$
Add more	First Then Now	I start at	plus is equal to
(augmentation)		I jump on I land on	is equal to +
A quantity is increased.	N. III byesy		4 + 2 = 6
		1 2 3 4 5 6 7 8 9 10	2 + 4 = 6
		0 1 2 3 4 5 6 7 8 9 10	6 = 4 + 2
			6 = 2 + 4



Progression of skills	Key representations		
Bonds within 10	is made of and and make	can be partitioned into and	plus is equal to $6 + 0 = 6$
Include bonds for each number within 10		6	5+3=6 $5+1=6$ $4+2=6$ $3+3=6$
Encourage children to notice patterns.			2 + 4 = 6 1 + 5 = 6 0 + 6 = 6
Related facts within 20	I know that and =	more than is	What patterns do you
Make links to known facts.	so and =	so more than is  0 1 2 3 4 5 6 7 8 9 10	notice? 5 + 2 = 7 15 + 2 = 17 7 = 5 + 2
		10 11 12 13 14 15 16 17 18 19 20	17 = 15 + 2
Missing numbers	How many more do you need to make?	If is the whole and is a part, the other part must	plus is equal to
Make links to known facts.		be 6 6 2 ?	2 +

### **Progression of skills - Subtraction**



Reception	Year 1	Year 2
<ul> <li>Conceptually subitise to 5</li> <li>1 less</li> <li>Notice the composition of numbers within 10</li> <li>Partition</li> <li>Take away</li> </ul>	<ul> <li>Find a part</li> <li>Take away</li> <li>Bonds within 10</li> <li>Related facts within 20</li> <li>Missing numbers</li> </ul>	<ul> <li>Subtract 1s from any number (related facts)</li> <li>Subtract across a 10</li> <li>Subtract multiples of 10</li> <li>Subtract 10s from any number</li> <li>Subtract two 2-digit numbers (not across a ten)</li> <li>Subtract two 2-digit numbers (across a ten)</li> <li>Missing numbers</li> </ul>



Year 1	<ul> <li>Read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs.</li> <li>Represent and use number bonds and related subtraction facts within 20</li> <li>Subtract one-digit and two-digit numbers to 20, including zero.</li> <li>Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 =  -9</li> </ul>				
Progression of skills	Key representations				
Find a part	There are in total are	is the whole is a part.	subtract is equal to is equal to —		
Link to number bonds and known facts. E.g. 2 + 4 = 6 so if 6 is the whole and 4 is a part, the other part must be 2	How many are <b>not</b> ?	is a part.	6-2=4 $6-4=2$ $4=6-2$ $2=6-4$		
Take away  A quantity is decreased.	First Then Now	I start at I jump back I land on	minus is equal to is equal to —		
11 5,250.000		1 2 3 4 5 6 7 8 9 10	6-2=4 6-4=2		
	4 = 6 - 2 $0 = 1 = 2 = 3 = 4$ $2 = 6 - 4$				



Progression of skills	Key representations		
Bonds within 10  Focus on subtraction facts.  Encourage children to notice patterns.	is made of and and make	can be partitioned into and	minus is equal to $6 - 0 = 6$ $6 - 1 = 5$ $6 - 2 = 4$ $6 - 3 = 3$ $6 - 4 = 2$ $6 - 5 = 1$ $6 - 6 = 0$
Related facts within 20  Make links to known facts.	I know that minus =  so minus =	less than is so less than is  0 1 2 3 4 5 6 7 8 9 10  10 11 12 13 14 15 16 17 18 19 20	What patterns do you notice? $8-3=5$ $18-3=15$ $5=8-3$ $15=18-3$
Missing numbers  Make links to known facts.	How many do you need to subtract to make?	If is the whole and is a part, the other part must be	minus is equal to $6 - \boxed{} = 2$ $2 = 6 - \boxed{}$

### **Progression of skills – Multiplication**



Reception	Year 1	Year 2
<ul> <li>Double to 10</li> <li>Make equal groups</li> </ul>	<ul> <li>Count in 2s, 5s and 10s</li> <li>Add equal groups</li> <li>Make arrays</li> <li>Make doubles</li> </ul>	<ul> <li>Link repeated addition and multiplication</li> <li>Use arrays</li> <li>Double</li> <li>The 2 times-table</li> <li>The 10 times-table</li> <li>The 5 times-table</li> <li>Missing numbers</li> </ul>



Marcipheacio	•			
Year 1	<ul> <li>Count in multiples of twos, fives and tens.</li> <li>Solve one-step problems involving multiplication, using concrete objects, pictorial representations and arrays with the support of the teacher.</li> </ul>			
Progression of skills	Key representations			
Count in 2s, 5s and 10s  Begin by counting objects that naturally come in 2s, 5s and 10s, for example pairs of socks or fingers.	There are equal groups of There are altogether.	1 2 3 4 11 12 13 14 1 21 22 23 24 2 31 32 33 34 3	5 6 7 8 9 10 15 16 17 18 19 20 25 26 27 28 29 30 35 36 37 38 39 40 45 46 47 48 49 50	Complete the number track/number line by counting ins.
Add equal groups (repeated addition)  Children should be able to write a repeated addition to represent equal groups and to draw pictures or use objects to represent a	There are groups of There are altogether.  10 + 10	+ 10 = 30 5 = 20	2 5 1	me? What is different? 2 + 2 + 2 = 5 + 5 + 5 = 0 + 10 + 10 = The a drawing to represent the

Use objects or a drawing to represent the equal groups and find how many in total.

repeated addition.



Progression of skills	Key representations			
Make arrays  Children use their knowledge of adding equal groups to arrange objects in columns and rows.	There are rows of There are altogether. There are columns of There are altogether.			
Make doubles  Children understand that doubles are two equal groups. Children may begin to explore doubles beyond 20 using base 10	Double is + =			

# Progression of skills – Division



Reception	Year 1 Year 2	
• Sharing	Make equal groups – grouping	Divide by 2
Grouping	Make equal groups – sharing	Divide by 10
	Find a half	Divide by 5
	Find a quarter	Missing numbers
		Unit fractions
		Non-unit fractions



Year 1	<ul> <li>Solve simple one-step problems involving division, using concrete objects, pictorial representations and arrays with the support of the teacher.</li> <li>Recognise, find and name a half as one of two equal parts of a quantity.</li> <li>Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.</li> </ul>			
Progression of skills	Key representations			
Make equal groups - grouping	There are altogether.  How many groups of can you make?  Circle groups of 2  Take cubes.  Make equal groups.			
Encourage children to physically move objects into equal groups. They can also circle equal groups when using pictures.		<b>₽ ₽</b> (	<b>} !</b>	There are groups of
Make equal groups – sharing	have been shared equally between There are on/in each		Take cubes. Share them be	
Encourage children to check that the objects have been shared fairly and each group				
is the same.			12 shared bet	ween is



Progression of skills	Key representations		
Find a half  Start with practical opportunities to share a quantity into 2 groups.  Progress to circling half of the objects in a picture and then to finding the whole from a given half.	To find half, I need to share into 2 equal groups.  There are in each group.	Half of is	If is half, what is the whole?  4 is half of
Find a quarter  Start with practical opportunities to share a quantity into 4 groups.  Progress to using pictures or bar models to find a quarter and then to finding the whole from a given quarter.	To find a quarter, I need to share into 4 equal groups.  There are in each group.	A quarter of is	If is one quarter, what is the whole?  ? 3 is one quarter of